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## QUESTION 31

**Choice D is the best answer.** The table clearly shows that the percentage of adenine in each organism's DNA is different, ranging from 24.7% in *E.coli* to 33.2% in the octopus. That such a variability would exist is predicted in lines 41-43, which states that "in a long molecule many different permutations are possible."

Choices A and B are incorrect because the table shows that the percentage of adenine varies between 24.7% and 33.2% in different organisms. Choice C is incorrect because lines 36-38 state that adenine pairs with thymine but does not mention the variability of the base composition of DNA.

## QUESTION 32

**Choice B is the best answer.** In this passage, Woolf asks women a series of questions. Woolf wants women to consider joining "the procession of educated men" (lines 56-57) by becoming members of the workforce. Woolf stresses that this issue is urgent, as women "have very little time in which to answer [these questions]" (lines 48-49).

Choice A is incorrect because Woolf argues against the tradition of only "the sons of educated men" (lines 82-83) joining the workforce. Choice C is incorrect because Woolf is not highlighting the severity of social divisions as much as she is explaining how those divisions might be reduced (with women joining the workforce). Choice D is incorrect because Woolf does not question the feasibility of changing the workforce dynamic.

## QUESTION 33

**Choice A is the best answer.** Throughout the passage, Woolf advocates for more women to engage with existing institutions by joining the workforce: "We too can leave the house, can mount those steps [to an office], pass in and out of those doors, . . . make money, administer justice . . ." (lines 30-32). Woolf tells educated women that they are at a "moment of transition" (line 51) where they must consider their future role in the workforce.

Choice B is incorrect because even though Woolf mentions women's traditional roles (lines 68-69: "while they stirred the pot, while they rocked the cradle"), she does not suggest that women will have to give up these traditional roles to gain positions of influence. Choice C is incorrect because though Woolf wonders how "the procession of the sons of educated men" impacts women's roles, she does not argue that this male-dominated society has had grave and continuing effects. Choice D is incorrect because while Woolf suggests educated women can hold positions currently held by men, she does not suggest that women's entry into positions of power will change those positions.

## QUESTION 34

**Choice C is the best answer.** Woolf uses the word “we” to refer to herself and educated women in English society, the “daughters of educated men” (line 64). Woolf wants these women to consider participating in a changing workforce: “For there, trapesing along at the tail end of the procession [to and from work], we go ourselves” (lines 23-24). In using the word “we” throughout the passage, Woolf establishes a sense of solidarity among educated women.

Choice A is incorrect because Woolf does not use “we” to reflect on whether people in a group are friendly to one another; she is concerned with generating solidarity among women. Choice B is incorrect because though Woolf admits women have predominantly “done their thinking” within traditional female roles (lines 64-69), she does not use “we” to advocate for more candor among women. Choice D is incorrect because Woolf does not use “we” to emphasize a need for people in a group to respect one other; rather, she wants to establish a sense of solidarity among women.

## QUESTION 35

**Choice B is the best answer.** Woolf argues that the “bridge over the River Thames, [has] an admirable vantage ground for us to make a survey” (lines 1-3). The phrase “make a survey” means to carefully examine an event or activity. Woolf wants educated women to “fix [their] eyes upon the procession — the procession of the sons of educated men” (lines 9-11) walking to work.

Choice A is incorrect because while Woolf states the bridge “is a place to stand on by the hour dreaming,” she states that she is using the bridge “to consider the facts” (lines 6-9). Woolf is not using the bridge for fanciful reflection; she is analyzing “the procession of the sons of educated men” (lines 10-11). Choice C is incorrect because Woolf does not compare the bridge to historic episodes. Choice D is incorrect because Woolf does not suggest that the bridge is a symbol of a male-dominated past, but rather that it serves as a good place to watch men proceed to work.

## QUESTION 36

**Choice D is the best answer.** Woolf writes that the men who conduct the affairs of the nation (lines 15-17: “ascending those pulpits, preaching, teaching, administering justice, practising medicine, transacting business, making money”) are the same men who go to and from work in a “procession” (line 10). Woolf notes that women are joining this procession, an act that suggests the workforce has become less exclusionary: “For there, trapesing along at the tail end of the procession, we go ourselves” (lines 23-24).

Choice A is incorrect because the procession is described as “a solemn sight always” (lines 17-18), which indicates that it has always been influential. Choice B is incorrect because the passage

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does not indicate that this procession has become a celebrated feature of English life. Choice C is incorrect because the passage states only that the procession is made up of “the sons of educated men” (lines 10-11).

### QUESTION 37

**Choice C is the best answer**, as lines 23-24 suggest that the workforce has become less exclusionary. In these lines Woolf describes how women are joining the male-dominated procession that travels to and from the work place: “For there, trapesing along at the tail end of the procession, we go ourselves.”

Choices A, B, and D are incorrect because they do not provide the best evidence for the answer to the previous question. Choice A is incorrect because lines 12-17 describe the positions predominantly held by men. Choice B is incorrect because lines 17-19 use a metaphor to describe how the procession physically looks.

Choice D is incorrect because lines 30-34 hypothesize about future jobs for women.

### QUESTION 38

**Choice C is the best answer.** Woolf characterizes the questions she asks in lines 53-57 as significant (“so important that they may well change the lives of all men and women for ever,” lines 52-53) and urgent (“we have very little time in which to answer them,” lines 48-49). Therefore, Woolf considers the questions posed in lines 53-57 as both momentous (significant) and pressing (urgent).

Choice A is incorrect because Woolf characterizes the questions as urgent and important, not as something that would cause controversy or fear. Choice B is incorrect because though Woolf considers the questions to be weighty (or “important”), she implies that they can be answered. Choice D is incorrect because Woolf does not imply that the questions are mysterious.

### QUESTION 39

**Choice B is the best answer.** The answer to the previous question shows how Woolf characterizes the questions posed in lines 53-57 as momentous and pressing. In lines 48-49, Woolf describes these questions as “important,” or momentous, and states that women “have very little time in which to answer them,” which shows their urgency.

Choices A, C, and D do not provide the best evidence for the answer to the previous question. Choices A and D are incorrect because lines 46-47 and line 62 suggest that women need to think about these questions and not offer trivial objections to them. Choice C is incorrect because line 57 characterizes only the need for urgency and does not mention the significance of the questions.

## QUESTION 40

**Choice C is the best answer.** Woolf writes that women “have thought” while performing traditional roles such as cooking and caring for children (lines 67-69). Woolf argues that this “thought” has shifted women’s roles in society and earned them a “brand-new sixpence” that they need to learn how to “spend” (lines 70-71). The “sixpence” mentioned in these lines is not a literal coin. Woolf is using the “sixpence” as a metaphor, as she is suggesting women take advantage of the opportunity to join the male-dominated workforce.

Choices A, B, and D are incorrect because in this context, “sixpence” does not refer to tolerance, knowledge, or perspective.

## QUESTION 41

**Choice B is the best answer.** In lines 72-76, Woolf repeats the phrase “let us think” to emphasize how important it is for women to critically reflect on their role in society. Woolf states this reflection can occur at any time: “Let us think in offices; in omnibuses; while we are standing in the crowd watching Coronations and Lord Mayor’s Shows; let us think . . . in the gallery of the House of Commons; in the Law Courts; let us think at baptisms and marriages and funerals.”

Choices A, C, and D are incorrect because in lines 72-76 Woolf is not emphasizing the novelty of the challenge faced by women, the complexity of social and political issues, or the enjoyable aspect of women’s career possibilities.

## QUESTION 42

**Choice B is the best answer.** The author of Passage 1 identifies specific companies such as the “Planetary Resources of Washington,” “Deep Space Industries of Virginia,” and “Golden Spike of Colorado” to support his earlier assertion that there are many interested groups “working to make space mining a reality” (line 8).

Choices A, C, and D are incorrect because the author of Passage 1 does not mention these companies to profile the technological advances in space mining, the profit margins from space mining, or the diverse approaches to space mining.

## QUESTION 43

**Choice A is the best answer.** The author of Passage 1 explicitly states that one benefit to space mining is access to precious metals and earth elements: “within a few decades, [space mining] may be meeting earthly demands for precious metals, such as platinum and gold, and the rare earth elements vital for personal electronics, such as yttrium and lanthanum” (lines 18-22).

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Choice B is incorrect because Passage 1 does not suggest that precious metals extracted from space may make metals more valuable on Earth. Choice C and Choice D are incorrect because Passage 1 never mentions how space mining could create unanticipated technological innovations or change scientists' understanding of space resources.

### QUESTION 44

**Choice A is the best answer.** Lines 18-22 suggest that space mining may help meet “earthly demands for precious metals . . . and the rare earth elements vital for personal electronics.” In this statement, the author is stating materials (“metals,” “earth elements”) that may be gathered as a result of space mining, and that these materials may be important to Earth’s economy.

Choices B, C, and D do not provide the best evidence for the answer to the previous question. Choice B is incorrect because lines 24-28 focus on an “off-planet economy” but never address positive effects of space mining. Choice C is incorrect because lines 29-30 suggest the relative value of water found in space. Choice D is incorrect because lines 41-44 state that space mining companies hope to find specific resources in lunar soil and asteroids but do not address how these resources are important to Earth’s economy.

### QUESTION 45

**Choice D is the best answer.** The author suggests in lines 19-22 that space mining may meet “earthly demands for precious metals, such as platinum and gold, and the rare earth elements vital for personal electronics.” In this sentence, “earthly demands” suggests that people want, or desire, these precious metals and rare earth elements.

Choices A, B, and C are incorrect because in this context “demands” does not mean offers, claims, or inquiries.

### QUESTION 46

**Choice C is the best answer.** Lines 29-30 introduce the idea that water mined in space may be very valuable: “water mined from other worlds could become the most desired commodity.” Lines 35-40 support this assertion by suggesting how mined space water could be used “for drinking or as a radiation shield” (lines 36-37) or to make “spacecraft fuel” (line 38).

Choice A is incorrect because the comparison in the previous paragraph (the relative value of gold and water to someone in the desert) is not expanded upon in lines 35-40. Choice B is incorrect because the question asked in the previous paragraph is also answered in that paragraph. Choice D is incorrect because no specific proposals are made in the previous paragraph; rather, an assertion is made and a question is posed.

## QUESTION 47

**Choice B is the best answer.** The author of Passage 2 recognizes that space mining may prove beneficial to humanity, stating that “we all stand to gain: the mineral bounty and spin-off technologies could enrich us all” (lines 50-52). The author also repeatedly mentions that space mining should be carefully considered before it is implemented: “But before the miners start firing up their rockets, we should pause for thought” (lines 53-54); “But [space mining’s] consequences — both here on Earth and in space — merit careful consideration” (lines 57-59).

Choice A is incorrect because the author of Passage 2 concedes that “space mining seems to sidestep most environmental concerns” (lines 55-56) but does not imply that space mining will recklessly harm the environment, either on Earth or in space. Choice C is incorrect because the author of Passage 2 does not address any key resources that may be disappearing on Earth. Choice D is incorrect because the author of Passage 2 admits that “resources that are valuable in orbit and beyond may be very different to those we prize on Earth” (lines 74-76) but does not mention any disagreement about the commercial viabilities of space mining discoveries.

## QUESTION 48

**Choice A is the best answer.** In lines 60-66, the author presents some environmental arguments against space mining: “[space] is not ours to despoil” and we should not “[glut] ourselves on space’s riches.” The author then suggests that these environmental arguments will be hard to “hold,” or maintain, when faced with the possible monetary rewards of space mining: “History suggests that those will be hard lines to hold . . .” (line 68).

Choices B, C, and D are incorrect because in this context, “hold” does not mean grip, restrain, or withstand.

## QUESTION 49

**Choice D is the best answer.** The author of Passage 1 is excited about the possibilities of space mining and how it can yield valuable materials, such as metals and elements (lines 19-20 and lines 41-42), water ice (line 35), and space dirt (line 44). The author of Passage 2, on the other hand, recognizes the possible benefits of space mining but also states that space mining should be thoughtfully considered before being implemented. Therefore, the author of Passage 2 expresses some concerns about a concept discussed in Passage 1.

Choice A is incorrect because the author of Passage 2 does not refute the central claim of Passage 1; both authors agree there are possible benefits to space mining. Choice B is incorrect because the author of Passage 1 does not describe space mining in more general terms than does the author of Passage 2. Choice C is incorrect because the author of Passage 2 is not suggesting that the space mining proposals stated in Passage 1 are impractical.

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## QUESTION 50

**Choice B is the best answer.** In lines 18-28, the author of Passage 1 describes many of the possible economic benefits of space mining, including the building of “an off-planet economy” (line 25). The author of Passage 2 warns that there may be ramifications to implementing space mining and building an “emerging off-world economy” (line 73) without regulation: “But miners have much to gain from a broad agreement on the for-profit exploitation of space. Without consensus, claims will be disputed, investments risky, and the gains made insecure” (lines 83-87).

Choices A, C, and D are incorrect because the author of Passage 2 does not suggest that the benefits to space mining mentioned in lines 18-28 of Passage 1 are unsustainable, unachievable, or will negatively affect Earth’s economy. Rather, the author recognizes the benefits of space mining but advocates for the development of regulation procedures.

## QUESTION 51

**Choice D is the best answer.** In lines 85-87, the author of Passage 2 states that the future of space mining will prove difficult without regulations because “claims will be disputed, investments risky, and the gains made insecure.”

Choices A, B, and C are incorrect because they do not provide the best evidence for the answer to the previous question. Choice A is incorrect because lines 60-63 present some environmental concerns toward space mining. Choice B is incorrect because lines 74-76 focus on how space mining may discover valuable resources that are different from the ones found on Earth. Choice C is incorrect because lines 81-83 simply describe one person’s objections to the regulation of the space mining industry.

## QUESTION 52

**Choice A is the best answer** because both Passage 1 and Passage 2 indicate a belief that the resources most valued in space may differ from those most valued on our planet. Passage 2 says this explicitly in lines 74-76: “The resources that are valuable in orbit and beyond may be very different to those we prize on Earth.” Meanwhile Passage 1 suggests that water mined from space may be more valuable than metals or other earth elements when creating an “off-plant economy” (lines 25-30).

Choice B is incorrect because neither passage discusses, either implicitly or explicitly, the need for space mining to be inexpensive. Choice C is incorrect because Passage 2 does not specifically identify precious metals or rare earth elements but instead focuses on theoretical problems with space mining. Choice D is incorrect because diminishing resources on Earth is not discussed in Passage 2.



## Section 2: Writing and Language Test

### QUESTION 1

**Choice D is the best answer** because “outweigh” is the only choice that appropriately reflects the relationship the sentence sets up between “advantages” and “drawbacks.”

Choices A, B, and C are incorrect because each implies a competitive relationship that is inappropriate in this context.

### QUESTION 2

**Choice B is the best answer** because it offers a second action that farmers can undertake to address the problem of acid whey disposal, thus supporting the claim made in the previous sentence (“To address the problem of disposal, farmers have found a *number of uses* for acid whey”).

Choices A, C, and D are incorrect because they do not offer examples of how farmers could make use of acid whey.

### QUESTION 3

**Choice A is the best answer** because it results in a sentence that is grammatically correct and coherent. In choice A, “waterways,” the correct plural form of “waterway,” conveys the idea that acid whey could impact multiple bodies of water. Additionally, the compound verb “can pollute” suggests that acid whey presents an ongoing, potential problem.

Choices B and D are incorrect because both use the possessive form of “waterway.” Choice C is incorrect because it creates an unnecessary shift in verb tense. The present tense verb “can pollute” should be used instead, as it is consistent with the other verbs in the paragraph.

### QUESTION 4

**Choice C is the best answer** because it utilizes proper punctuation for items listed in a series. In this case those items are nouns: “Yogurt manufacturers, food scientists, and government officials.”

Choices A and B are incorrect because both fail to recognize that the items are a part of a series. Since a comma is used after “manufacturers,” a semicolon or colon should not be used after “scientists.” Choice D is incorrect because the comma after “and” is unnecessary and deviates from grammatical conventions for presenting items in a series.

### QUESTION 5

**Choice C is the best answer** because sentence 5 logically links sentence 2, which explains why Greek yogurt production yields large amounts of acid whey, and sentence 3, which mentions the need to dispose of acid whey properly.

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Choices A, B, and D are incorrect because each would result in an illogical progression of sentences for this paragraph. If sentence 5 were left where it is or placed after sentence 3, it would appear illogically after the discussion of “the problem of disposal.” If sentence 5 were placed after sentence 1, it would illogically discuss “acid-whey runoff” before the mention of acid whey being “difficult to dispose of.”

## QUESTION 6

**Choice D is the best answer** because the paragraph includes several benefits of consuming Greek yogurt, particularly in regard to nutrition and satisfying hunger, to support the sentence’s claim that the conservation efforts are “well worth the effort.” This transition echoes the passage’s earlier claim that “the advantages of Greek yogurt outweigh the potential drawbacks of its production.”

Choices A, B, and C are incorrect because they inaccurately describe the sentence in question.

## QUESTION 7

**Choice B is the best answer** because it provides a grammatically standard preposition that connects the verb “serves” and noun “digestive aid” and accurately depicts their relationship.

Choice A is incorrect because the infinitive form “to be” yields a grammatically incorrect verb construction: “serves to be.” Choices C and D are incorrect because both present options that deviate from standard English usage.

## QUESTION 8

**Choice C is the best answer** because it presents a verb tense that is consistent in the context of the sentence. The choice is also free of the redundant “it.”

Choice A is incorrect because the subject “it” creates a redundancy. Choices B and D are incorrect because they present verb tenses that are inconsistent in the context of the sentence.

## QUESTION 9

**Choice A is the best answer** because it properly introduces an additional health benefit in a series of sentences that list health benefits. “Also” is the logical and coherent choice to communicate an addition.

Choices B, C, and D are incorrect because none of the transitions they offer logically fits the content that precedes or follows the proposed choice.

## QUESTION 10

**Choice A is the best answer** because “satiated” is the only choice that communicates effectively that Greek yogurt will satisfy hunger for a longer period of time.

Choices B, C, and D are incorrect because each is improper usage in this context. A person can be “fulfilled” spiritually or in other ways, but a person who has eaten until he or she is no longer hungry cannot be described as fulfilled. Neither can he or she be described as being “complacent” or “sufficient.”

### QUESTION 11

**Choice B is the best answer** because it provides a syntactically coherent and grammatically correct sentence.

Choices A and C are incorrect because the adverbial conjunctions “therefore” and “so,” respectively, are unnecessary following “Because.” Choice D is incorrect because it results in a grammatically incomplete sentence (the part of the sentence before the colon must be an independent clause).

### QUESTION 12

**Choice B is the best answer** because the graph clearly indicates that, on March 5, average low temperatures are at their lowest point: 12 degrees Fahrenheit.

Choice A is incorrect because the phrase “as low as” suggests that the temperature falls no lower than 20 degrees Fahrenheit, but the chart shows that in January, February, and March, the temperature frequently falls below that point. Choices C and D are incorrect because the information each provides is inconsistent with the information on the chart.

### QUESTION 13

**Choice A is the best answer** because it concisely combines the two sentences while maintaining the original meaning.

Choices B, C, and D are incorrect because each is unnecessarily wordy, thus undermining one purpose of combining two sentences: to make the phrasing more concise.

### QUESTION 14

**Choice B is the best answer** because it provides a conjunctive adverb that accurately represents the relationship between the two sentences. “However” signals an exception to a case stated in the preceding sentence.

Choices A, C, and D are incorrect because each provides a transition that does not accurately represent the relationship between the two sentences, and as a result each compromises the logical coherence of these sentences.

### QUESTION 15

**Choice C is the best answer** because it provides commas to offset the nonrestrictive modifying clause “an associate professor of geology at Ohio State.”

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Choices A, B, and D are incorrect because each provides punctuation that does not adequately separate the nonrestrictive modifying clause about Jason Box from the main clause.

### QUESTION 16

**Choice C is the best answer** because the colon signals that the other factor that contributed to the early thaw is about to be provided.

Choice A is incorrect because it results in a sentence that deviates from grammatical standards: a semicolon should be used to separate two independent clauses, but in choice A the second clause only has a subject, not a verb. Choice B is incorrect because it is unnecessarily wordy. Choice D is incorrect because “being” is unnecessary and creates an incoherent clause.

### QUESTION 17

**Choice C is the best answer** because it provides the correct preposition (“of”) and relative pronoun (“which”) that together create a dependent clause following the comma.

Choices A, B, and D are incorrect because each results in a comma splice. Two independent clauses cannot be joined with only a comma.

### QUESTION 18

**Choice A is the best answer** because the verb tense is consistent with the preceding past tense verbs in the sentence, specifically “produced” and “drifted.”

Choices B, C, and D are incorrect because each utilizes a verb tense that is not consistent with the preceding past tense verbs in the sentence.

### QUESTION 19

**Choice D is the best answer** because “their” is the possessive form of a plural noun. In this case, the noun is plural: “snow and ice.”

Choices A and B are incorrect because the possessive pronoun must refer to a plural noun, “snow and ice,” rather than a singular noun. Choice C is incorrect because “there” would result in an incoherent sentence.

### QUESTION 20

**Choice D is the best answer.** The preceding sentences in the paragraph have established that a darker surface of soot-covered snow leads to more melting because this darker surface absorbs heat, whereas a whiter surface, free of soot, would deflect heat. As the passage points out, exposed land and water are also dark and cannot deflect heat the way ice and snow can. Only choice D reflects the self-reinforcing cycle that the preceding sentences already imply.

Choices A, B, and C are incorrect because the information each provides fails to support the previous claim that the “result” of the soot “is a self-reinforcing cycle.”

### QUESTION 21

**Choice B is the best answer** because it is free of redundancies.

Choices A, C, and D are incorrect because each of the three presents a redundancy: Choice A uses “repeat” and “again”; Choice C uses “damage” and “harmful effects”; and Choice D uses “may” and “possibly.”

### QUESTION 22

**Choice D is the best answer** because sentence 5 describes the information Box seeks: “to determine just how much the soot is contributing to the melting of the ice sheet.” Unless sentence 4 comes after sentence 5, readers will not know what the phrase “this crucial information” in sentence 4 refers to.

Choices A, B, and C are incorrect because each results in an illogical sentence progression. None of the sentences that would precede sentence 4 provides details that could be referred to as “this crucial information.”

### QUESTION 23

**Choice D is the best answer** because it is free of redundancies and offers the correct form of the verb “wear” in this context.

Choices A, B, and C are incorrect because all three contain a redundancy. Considering that “quickly” is a fixed part of the sentence, choice A’s “soon” and choice B and C’s “promptly” all result in redundancies. Choices A and B are also incorrect because each uses an incorrect form of the verb.

### QUESTION 24

**Choice D is the best answer** because it is the only choice that provides a grammatically standard and coherent sentence. The participial phrase “Having become frustrated. . .” functions as an adjective modifying “I,” the writer.

Choices A, B, and C are incorrect because each results in a dangling modifier. The participial phrase “Having become frustrated . . .” does not refer to choice A’s “no colleagues,” choice B’s “colleagues,” or choice C’s “ideas.” As such, all three choices yield incoherent and grammatically incorrect sentences.

### QUESTION 25

**Choice B is the best answer** because it provides the correct preposition in this context, “about.”

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Choices A, C, and D are incorrect because each provides a preposition that deviates from correct usage. One might read an article “about” coworking spaces but not an article “into,” “upon,” or “for” coworking spaces.

### QUESTION 26

**Choice A is the best answer** because it provides the correct punctuation for the dependent clause that begins with the phrase “such as.”

Choices B, C, and D are incorrect because each presents punctuation that deviates from the standard way of punctuating the phrase “such as.” When “such as” is a part of a nonrestrictive clause, as it is here, only one comma is needed to separate it from the main independent clause.

### QUESTION 27

**Choice B is the best answer** because it provides a transitional phrase, “In addition to equipment,” that accurately represents the relationship between the two sentences connected by the transitional phrase. Together, the sentences describe the key features of coworking spaces, focusing on what the spaces offer (equipment and meeting rooms).

Choices A, C, and D are incorrect because each provides a transition that does not accurately represent the relationship between the two sentences.

### QUESTION 28

**Choice C is the best answer** because the sentence is a distraction from the paragraph’s focus. Nothing in the paragraph suggests that the cost of setting up a coworking business is relevant here.

Choices A and D are incorrect because neither accurately represents the information in the paragraph. Choice B is incorrect because it does not accurately represent the information in the next paragraph.

### QUESTION 29

**Choice B is the best answer** because it logically follows the writer’s preceding statement about creativity and accurately represents the information in the graph.

Choices A, C, and D are incorrect because they present inaccurate and unsupported interpretations of the information in the graph. In addition, none of these choices provides directly relevant support for the main topic of the paragraph.

### QUESTION 30

**Choice D is the best answer** because it provides a relative pronoun and verb that create a standard and coherent sentence. The relative pronoun “who” refers to the subject “the people,” and the plural verb “use” corresponds grammatically with the plural noun “people.”

Choices A and B are incorrect because “whom” is the relative pronoun used to represent an object. The noun “people” is a subject performing an action (using the coworking space). Choices B and C are also incorrect because they display a form of the verb “to use” that does not correspond to the plural noun “people.”

### QUESTION 31

**Choice C is the best answer** because the proposed sentence offers a necessary and logical transition between sentence 2, which introduces the facility the writer chose, and sentence 3, which tells what happened at the facility “Throughout the morning.”

Choices A, B, and D are incorrect because each would result in an illogical progression of sentences.

### QUESTION 32

**Choice A is the best answer** because the punctuation it provides results in a grammatically standard and coherent sentence. When an independent clause is followed by a list, a colon is used to link the two.

Choice B is incorrect because the punctuation creates a fragment (a semicolon should be used to link two independent clauses).

Choice C is incorrect because its use of the comma creates a series in which “several of my coworking colleagues” are distinguished from the “website developer” and others, although the logic of the sentence would suggest that they are the same. Choice D is incorrect because it lacks the punctuation necessary to link the independent clause and the list.

### QUESTION 33

**Choice A is the best answer** because it provides a phrase that is consistent with standard English usage and also maintains the tone and style of the passage.

Choice B is incorrect because “give some wisdom” deviates from standard English usage and presents a somewhat colloquial phrase in a text that is generally free of colloquialisms. Choices C and D are incorrect because both are inconsistent with the tone of the passage as well as its purpose. The focus of the paragraph is on sharing, not on proclaiming opinions.

### QUESTION 34

**Choice A is the best answer** because it offers a phrase that introduces a basic definition of philosophy and thereby fits the sentence.

Choices B, C, and D are incorrect because each offers a transition that does not suit the purpose of the sentence.

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## QUESTION 35

**Choice A is the best answer** because it offers the most succinct comparison between the basic definition of philosophy and the fact that students can gain specific, practical skills from the study of philosophy. There is no need to include the participle “speaking” in this sentence, as it is clear from context that the writer is offering a different perspective.

Choices B, C, and D are incorrect because they provide options that are unnecessarily wordy.

## QUESTION 36

**Choice B is the best answer** because it provides a verb that creates a grammatically complete, standard, and coherent sentence.

Choices A, C, and D are incorrect because each results in a grammatically incomplete and incoherent sentence.

## QUESTION 37

**Choice D is the best answer** because it most effectively sets up the information in the following sentences, which state that (according to information from the 1990s) “only 18 percent of American colleges required at least one philosophy course,” and “more than 400 independent philosophy departments were eliminated” from colleges. These details are most logically linked to the claim that “colleges have not always supported the study of philosophy.”

Choices A, B, and C are incorrect because none of these effectively sets up the information that follows, which is about colleges’ failure to support the study of philosophy.

## QUESTION 38

**Choice C is the best answer** because it provides a transition that logically connects the information in the previous sentence to the information in this one. Both sentences provide evidence of colleges’ lack of support of philosophy programs, so the adverb “Moreover,” which means “In addition,” accurately captures the relationship between the two sentences.

Choices A, B, and D are incorrect because each presents a transition that does not accurately depict or support the relationship between the two sentences. The second sentence is not a result of the first (“Therefore,” “Thus”), and the sentences do not provide a contrast (“However”).

## QUESTION 39

**Choice A is the best answer** because it succinctly expresses the idea that “students who major in philosophy often do better . . . as measured by standardized test scores.”



Choices B and D are incorrect because they introduce a redundancy and a vague term, “results.” The first part of the sentence mentions a research finding or conclusion but does not directly address any “results,” so it is confusing to refer to “these results” and indicate that they “can be” or “are measured by standardized test scores.” The best way to express the idea is simply to say that some students “often do better” than some other students “in both verbal reasoning and analytical writing as measured by standardized test scores.” Choice C is incorrect because there is no indication that multiple criteria are used to evaluate students’ “verbal reasoning and analytical writing”: test scores and something else. Only test scores are mentioned.

## QUESTION 40

**Choice B is the best answer** because it provides subject-verb agreement and thus creates a grammatically correct and coherent sentence.

Choice A is incorrect because the verb “has scored” does not correspond with the plural subject “students.” Similarly, Choice C is incorrect because the verb “scores” would correspond with a singular subject, but not the plural subject present in this sentence. Choice D is incorrect because it results in a grammatically incomplete and incoherent sentence.

## QUESTION 41

**Choice B is the best answer** because it provides a coherent and grammatically standard sentence.

Choices A and D are incorrect because both present “students” in the possessive form, whereas the sentence establishes “students” as the subject (“many students . . . have”). Choice C is incorrect because the verb form it proposes results in an incomplete and incoherent sentence.

## QUESTION 42

**Choice C is the best answer** because it accurately depicts how inserting this sentence would affect the overall paragraph. The fact that Plato used the dialogue form has little relevance to the preceding claim about the usefulness of a philosophy background.

Choices A and B are incorrect because the proposed sentence interrupts the progression of reasoning in the paragraph. Choice D is incorrect because, as with Choice A, Plato’s works have nothing to do with “the employability of philosophy majors.”

## QUESTION 43

**Choice D is the best answer** because it creates a complete and coherent sentence.

Choices A, B, and C are incorrect because each inserts an unnecessary relative pronoun or conjunction, resulting in a sentence without a main verb.

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## QUESTION 44

**Choice D is the best answer** because it provides a possessive pronoun that is consistent with the sentence’s plural subject “students,” thus creating a grammatically sound sentence.

Choices A, B, and C are incorrect because each proposes a possessive pronoun that is inconsistent with the plural noun “students,” the established subject of the sentence.

## Section 3: Math Test – No Calculator

### QUESTION 1

**Choice D is correct.** Since  $k = 3$ , one can substitute 3 for  $k$  in the equation  $\frac{x-1}{3} = k$ , which gives  $\frac{x-1}{3} = 3$ . Multiplying both sides of  $\frac{x-1}{3} = 3$  by 3 gives  $x - 1 = 9$  and then adding 1 to both sides of  $x - 1 = 9$  gives  $x = 10$ .

Choices A, B, and C are incorrect because the result of subtracting 1 from the value and dividing by 3 is not the given value of  $k$ , which is 3.

### QUESTION 2

**Choice A is correct.** To calculate  $(7 + 3i) + (-8 + 9i)$ , add the real parts of each complex number,  $7 + (-8) = -1$ , and then add the imaginary parts,  $3i + 9i = 12i$ . The result is  $-1 + 12i$ .

Choices B, C, and D are incorrect and likely result from common errors that arise when adding complex numbers. For example, choice B is the result of adding  $3i$  and  $-9i$ , and choice C is the result of adding 7 and 8.

### QUESTION 3

**Choice C is correct.** The total number of text messages sent by Armand can be found by multiplying his rate of texting, in number of text messages sent per hour, by the total number of hours he spent sending them; that is  $m$  texts/hour  $\times$  5 hours  $= 5m$  texts. Similarly, the total number of text messages sent by Tyrone is his hourly rate of texting multiplied by the 4 hours he spent texting:  $p$  texts/hour  $\times$  4 hours  $= 4p$  texts. The total number of text messages sent by Armand and Tyrone is the sum of the total number of messages sent by Armand and the total number of messages sent by Tyrone:  $5m + 4p$ .

Choice A is incorrect and arises from adding the coefficients and multiplying the variables of  $5m$  and  $4p$ . Choice B is incorrect and is the result of multiplying  $5m$  and  $4p$ . The total number of messages sent by Armand and Tyrone should be the sum of  $5m$  and  $4p$ , not the product of these terms. Choice D is incorrect because it multiplies Armand’s number of hours spent texting by Tyrone’s hourly rate of

texting, and vice versa. This mix-up results in an expression that does not equal the total number of messages sent by Armand and Tyrone.

### QUESTION 4

**Choice B is correct.** The value 108 in the equation is the value of  $P$  in  $P = 108 - 23d$  when  $d = 0$ . When  $d = 0$ , Kathy has worked 0 days that week. In other words, 108 is the number of phones left before Kathy has started work for the week. Therefore, the meaning of the value 108 in the equation is that Kathy starts each week with 108 phones to fix.

Choice A is incorrect because Kathy will complete the repairs when  $P = 0$ . Since  $P = 108 - 23d$ , this will occur when  $0 = 108 - 23d$  or when  $d = \frac{108}{23}$ , not when  $d = 108$ . Therefore, the value 108 in the equation

does not represent the number of days it will take Kathy to complete the repairs. Choices C and D are incorrect because the number 23 in  $P = 108 - 23d$  indicates that the number of phones left will decrease by 23 for each increase in the value of  $d$  by 1; in other words, Kathy is repairing phones at a rate of 23 per day, not 108 per hour (choice C) or 108 per day (choice D).

### QUESTION 5

**Choice C is correct.** Only like terms, with the same variables and exponents, can be combined to determine the answer as shown here:

$$\begin{aligned} & (x^2y - 3y^2 + 5xy^2) - (-x^2y + 3xy^2 - 3y^2) \\ &= (x^2y - (-x^2y)) + (-3y^2 - (-3y^2)) + (5xy^2 - 3xy^2) \\ &= 2x^2y + 0 + 2xy^2 \\ &= 2x^2y + 2xy^2 \end{aligned}$$

Choices A, B, and D are incorrect and are the result of common calculation errors or of incorrectly combining like and unlike terms.

### QUESTION 6

**Choice A is correct.** In the equation  $h = 3a + 28.6$ , if  $a$ , the age of the boy, increases by 1, then  $h$  becomes  $h = 3(a + 1) + 28.6 = 3a + 3 + 28.6 = (3a + 28.6) + 3$ . Therefore, the model estimates that the boy's height increases by 3 inches each year.

Alternatively: The height,  $h$ , is a linear function of the age,  $a$ , of the boy. The coefficient 3 can be interpreted as the rate of change of the function; in this case, the rate of change can be described as a change of 3 inches in height for every additional year in age.

Choices B, C, and D are incorrect and are likely the result of dividing 28.6 by 5, 3, and 2, respectively. The number 28.6 is the estimated height, in inches, of a newborn boy. However, dividing 28.6 by 5, 3, or 2 has no meaning in the context of this question.

## QUESTION 7

**Choice B is correct.** Since the right-hand side of the equation is

$P$  times the expression  $\frac{\left(\frac{r}{1,200}\right)\left(1 + \frac{r}{1,200}\right)^N}{\left(1 + \frac{r}{1,200}\right)^N - 1}$ , multiplying both

sides of the equation by the reciprocal of this expression results

in  $\frac{\left(1 + \frac{r}{1,200}\right)^N - 1}{\left(\frac{r}{1,200}\right)\left(1 + \frac{r}{1,200}\right)^N} m = P$ .

Choice A is incorrect and is the result of multiplying both sides of the

equation by the rational expression  $\frac{\left(\frac{r}{1,200}\right)\left(1 + \frac{r}{1,200}\right)^N}{\left(1 + \frac{r}{1,200}\right)^N - 1}$  rather than

by the reciprocal of this expression  $\frac{\left(1 + \frac{r}{1,200}\right)^N - 1}{\left(\frac{r}{1,200}\right)\left(1 + \frac{r}{1,200}\right)^N}$ . Choices C

and D are incorrect and are likely the result of errors while trying to solve for  $P$ .

## QUESTION 8

**Choice C is correct.** Since  $\frac{a}{b} = 2$ , it follows that  $\frac{b}{a} = \frac{1}{2}$ . Multiplying both

sides of the equation by 4 gives  $4\left(\frac{b}{a}\right) = 4\left(\frac{1}{2}\right)$ , or  $\frac{4b}{a} = 2$ .

Choice A is incorrect because if  $\frac{4b}{a} = 0$ , then  $\frac{a}{b}$  would be undefined.

Choice B is incorrect because if  $\frac{4b}{a} = 1$ , then  $\frac{a}{b} = 4$ . Choice D is

incorrect because if  $\frac{4b}{a} = 4$ , then  $\frac{a}{b} = 1$ .

## QUESTION 9

**Choice B is correct.** Adding  $x$  and 19 to both sides of  $2y - x = -19$  gives  $x = 2y + 19$ . Then, substituting  $2y + 19$  for  $x$  in  $3x + 4y = -23$  gives  $3(2y + 19) + 4y = -23$ . This last equation is equivalent to  $10y + 57 = -23$ . Solving  $10y + 57 = -23$  gives  $y = -8$ . Finally, substituting  $-8$  for  $y$  in  $2y - x = -19$  gives  $2(-8) - x = -19$ , or  $x = 3$ . Therefore, the solution  $(x, y)$  to the given system of equations is  $(3, -8)$ .

Choices A, C, and D are incorrect because when the given values of  $x$  and  $y$  are substituted in  $2y - x = -19$ , the value of the left side of the equation does not equal  $-19$ .

## QUESTION 10

**Choice A is correct.** Since  $g$  is an even function,  $g(-4) = g(4) = 8$ .

Alternatively: First find the value of  $a$ , and then find  $g(-4)$ .

Since  $g(4) = 8$ , substituting 4 for  $x$  and 8 for  $g(x)$  gives

$8 = a(4)^2 + 24 = 16a + 24$ . Solving this last equation gives  $a = -1$ .

Thus  $g(x) = -x^2 + 24$ , from which it follows that

$g(-4) = -(-4)^2 + 24$ ;  $g(-4) = -16 + 24$ ; and  $g(-4) = 8$ .

Choices B, C, and D are incorrect because  $g$  is a function and there can only be one value of  $g(-4)$ .

### QUESTION 11

**Choice D is correct.** To determine the price per pound of beef when it was equal to the price per pound of chicken, determine the value of  $x$  (the number of weeks after July 1) when the two prices were equal. The prices were equal when  $b = c$ ; that is, when  $2.35 + 0.25x = 1.75 + 0.40x$ . This last equation is equivalent to  $0.60 = 0.15x$ , and so  $x = \frac{0.60}{0.15} = 4$ . Then to determine  $b$ , the price per pound of beef, substitute 4 for  $x$  in  $b = 2.35 + 0.25x$ , which gives  $b = 2.35 + 0.25(4) = 3.35$  dollars per pound.

Choice A is incorrect. It results from substituting the value 1, not 4, for  $x$  in  $b = 2.35 + 0.25x$ . Choice B is incorrect. It results from substituting the value 2, not 4, for  $x$  in  $b = 2.35 + 0.25x$ . Choice C is incorrect. It results from substituting the value 3, not 4, for  $x$  in  $c = 1.75 + 0.40x$ .

### QUESTION 12

**Choice D is correct.** In the  $xy$ -plane, all lines that pass through the origin are of the form  $y = mx$ , where  $m$  is the slope of the line. Therefore, the equation of this line is  $y = \frac{1}{7}x$ , or  $x = 7y$ . A point with coordinates  $(a, b)$  will lie on the line if and only if  $a = 7b$ . Of the given choices, only choice D,  $(14, 2)$ , satisfies this condition:  $14 = 7(2)$ . Choice A is incorrect because the line determined by the origin  $(0, 0)$  and  $(0, 7)$  is the vertical line with equation  $x = 0$ ; that is, the  $y$ -axis. The slope of the  $y$ -axis is undefined, not  $\frac{1}{7}$ . Therefore, the point  $(0, 7)$  does not lie on the line that passes the origin and has slope  $\frac{1}{7}$ . Choices B and C are incorrect because neither of the ordered pairs has a  $y$ -coordinate that is  $\frac{1}{7}$  the value of the corresponding  $x$ -coordinate.

### QUESTION 13

**Choice B is correct.** To rewrite  $\frac{1}{\frac{1}{x+2} + \frac{1}{x+3}}$ , multiply by  $\frac{(x+2)(x+3)}{(x+2)(x+3)}$ . This results in the expression  $\frac{(x+2)(x+3)}{(x+2) + (x+3)}$ , which is equivalent to the expression in choice B.

Choices A, C, and D are incorrect and could be the result of common algebraic errors that arise while manipulating a complex fraction.

### QUESTION 14

**Choice A is correct.** One approach is to express  $\frac{8^x}{2^y}$  so that the numerator and denominator are expressed with the same base. Since 2 and 8 are both powers of 2, substituting  $2^3$  for 8 in the numerator

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of  $\frac{8^x}{2^y}$  gives  $\frac{(2^3)^x}{2^y}$ , which can be rewritten as  $\frac{2^{3x}}{2^y}$ . Since the numerator and denominator of  $\frac{2^{3x}}{2^y}$  have a common base, this expression can be rewritten as  $2^{3x-y}$ . It is given that  $3x - y = 12$ , so one can substitute 12 for the exponent,  $3x - y$ , given that the expression  $\frac{8^x}{2^y}$  is equal to  $2^{12}$ .

Choice B is incorrect. The expression  $\frac{8^x}{2^y}$  can be rewritten as  $\frac{2^{3x}}{2^y}$ , or  $2^{3x-y}$ . If the value of  $2^{3x-y}$  is  $4^4$ , which can be rewritten as 28, then  $2^{3x-y} = 2^8$ , which results in  $3x - y = 8$ , not 12. Choice C is incorrect. If the value of  $\frac{8^x}{2^y}$  is  $8^2$ , then  $2^{3x-y} = 8^2$ , which results in  $3x - y = 6$ , not 12. Choice D is incorrect because the value of  $\frac{8^x}{2^y}$  can be determined.

### QUESTION 15

**Choice D is correct.** One can find the possible values of  $a$  and  $b$  in  $(ax + 2)(bx + 7)$  by using the given equation  $a + b = 8$  and finding another equation that relates the variables  $a$  and  $b$ . Since  $(ax + 2)(bx + 7) = 15x^2 + cx + 14$ , one can expand the left side of the equation to obtain  $abx^2 + 7ax + 2bx + 14 = 15x^2 + cx + 14$ . Since  $ab$  is the coefficient of  $x^2$  on the left side of the equation and 15 is the coefficient of  $x^2$  on the right side of the equation, it must be true that  $ab = 15$ . Since  $a + b = 8$ , it follows that  $b = 8 - a$ . Thus,  $ab = 15$  can be rewritten as  $a(8 - a) = 15$ , which in turn can be rewritten as  $a^2 - 8a + 15 = 0$ . Factoring gives  $(a - 3)(a - 5) = 0$ . Thus, either  $a = 3$  and  $b = 5$ , or  $a = 5$  and  $b = 3$ . If  $a = 3$  and  $b = 5$ , then  $(ax + 2)(bx + 7) = (3x + 2)(5x + 7) = 15x^2 + 31x + 14$ . Thus, one of the possible values of  $c$  is 31. If  $a = 5$  and  $b = 3$ , then  $(ax + 2)(bx + 7) = (5x + 2)(3x + 7) = 15x^2 + 41x + 14$ . Thus, another possible value for  $c$  is 41. Therefore, the two possible values for  $c$  are 31 and 41.

Choice A is incorrect; the numbers 3 and 5 are possible values for  $a$  and  $b$ , but not possible values for  $c$ . Choice B is incorrect; if  $a = 5$  and  $b = 3$ , then 6 and 35 are the coefficients of  $x$  when the expression  $(5x + 2)(3x + 7)$  is expanded as  $15x^2 + 35x + 6x + 14$ . However, when the coefficients of  $x$  are 6 and 35, the value of  $c$  is 41 and not 6 and 35. Choice C is incorrect; if  $a = 3$  and  $b = 5$ , then 10 and 21 are the coefficients of  $x$  when the expression  $(3x + 2)(5x + 7)$  is expanded as  $15x^2 + 21x + 10x + 14$ . However, when the coefficients of  $x$  are 10 and 21, the value of  $c$  is 31 and not 10 and 21.

### QUESTION 16

**The correct answer is 2.** To solve for  $t$ , factor the left side of  $t^2 - 4 = 0$ , giving  $(t - 2)(t + 2) = 0$ . Therefore, either  $t - 2 = 0$  or  $t + 2 = 0$ . If  $t - 2 = 0$ , then  $t = 2$ , and if  $t + 2 = 0$ , then  $t = -2$ . Since it is given that  $t > 0$ , the value of  $t$  must be 2.

Another way to solve for  $t$  is to add 4 to both sides of  $t^2 - 4 = 0$ , giving  $t^2 = 4$ . Then, taking the square root of the left and the right side of the equation gives  $t = \pm\sqrt{4} = \pm 2$ . Since it is given that  $t > 0$ , the value of  $t$  must be 2.

## QUESTION 17

**The correct answer is 1600.** It is given that  $\angle AEB$  and  $\angle CDB$  have the same measure. Since  $\angle ABE$  and  $\angle CBD$  are vertical angles, they have the same measure. Therefore, triangle  $EAB$  is similar to triangle  $DCB$  because the triangles have two pairs of congruent corresponding angles (angle-angle criterion for similarity of triangles). Since the triangles are similar, the corresponding sides are in the same proportion; thus  $\frac{CD}{x} = \frac{BD}{EB}$ . Substituting the given values of 800 for  $CD$ , 700 for  $BD$ , and 1400 for  $EB$  in  $\frac{CD}{x} = \frac{BD}{EB}$  gives  $\frac{800}{x} = \frac{700}{1400}$ . Therefore,  $x = \frac{(800)(1400)}{700} = 1600$ .

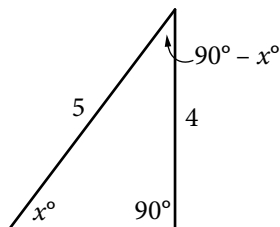
## QUESTION 18

**The correct answer is 7.** Subtracting the left and right sides of  $x + y = -9$  from the corresponding sides of  $x + 2y = -25$  gives  $(x + 2y) - (x + y) = -25 - (-9)$ , which is equivalent to  $y = -16$ . Substituting  $-16$  for  $y$  in  $x + y = -9$  gives  $x + (-16) = -9$ , which is equivalent to  $x = -9 - (-16) = 7$ .

## QUESTION 19

**The correct answer is  $\frac{4}{5}$  or 0.8.** By the complementary angle relationship for sine and cosine,  $\sin(x^\circ) = \cos(90^\circ - x^\circ)$ . Therefore,  $\cos(90^\circ - x^\circ) = \frac{4}{5}$ . Either the fraction  $\frac{4}{5}$  or its decimal equivalent, 0.8, may be gridded as the correct answer.

Alternatively, one can construct a right triangle that has an angle of measure  $x^\circ$  such that  $\sin(x^\circ) = \frac{4}{5}$ , as shown in the figure below, where  $\sin(x^\circ)$  is equal to the ratio of the length of the side opposite the angle measuring  $x^\circ$  to the length of the hypotenuse, or  $\frac{4}{5}$ .



Since two of the angles of the triangle are of measure  $x^\circ$  and  $90^\circ$ , the third angle must have the measure  $180^\circ - 90^\circ - x^\circ = 90^\circ - x^\circ$ . From the figure,  $\cos(90^\circ - x^\circ)$ , which is equal to the ratio of the length of the side adjacent to the angle measuring  $90^\circ - x^\circ$  to the hypotenuse, is also  $\frac{4}{5}$ .

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## QUESTION 20

**The correct answer is 100.** Since  $a = 5\sqrt{2}$ , one can substitute  $5\sqrt{2}$  for  $a$  in  $2a = \sqrt{2x}$ , giving  $10\sqrt{2} = \sqrt{2x}$ . Squaring each side of  $10\sqrt{2} = \sqrt{2x}$  gives  $(10\sqrt{2})^2 = (\sqrt{2x})^2$ , which simplifies to  $(10)^2(\sqrt{2})^2 = (\sqrt{2x})^2$ , or  $200 = 2x$ . This gives  $x = 100$ . To verify, substitute 100 for  $x$  and  $5\sqrt{2}$  for  $a$  in the equation  $2a = \sqrt{2x}$ , which yields  $2(5\sqrt{2}) = \sqrt{(2)(100)}$ ; this is true since  $2(5\sqrt{2}) = 10\sqrt{2}$  and  $\sqrt{(2)(100)} = \sqrt{2}\sqrt{100} = 10\sqrt{2}$ .

## Section 4: Math Test – Calculator

### QUESTION 1

**Choice B is correct.** On the graph, a line segment with a positive slope represents an interval over which the target heart rate is strictly increasing as time passes. A horizontal line segment represents an interval over which there is no change in the target heart rate as time passes, and a line segment with a negative slope represents an interval over which the target heart rate is strictly decreasing as time passes. Over the interval between 40 and 60 minutes, the graph consists of a line segment with a positive slope followed by a line segment with a negative slope, with no horizontal line segment in between, indicating that the target heart rate is strictly increasing then strictly decreasing.

Choice A is incorrect because the graph over the interval between 0 and 30 minutes contains a horizontal line segment, indicating a period in which there was no change in the target heart rate. Choice C is incorrect because the graph over the interval between 50 and 65 minutes consists of a line segment with a negative slope followed by a line segment with a positive slope, indicating that the target heart rate is strictly decreasing then strictly increasing. Choice D is incorrect because the graph over the interval between 70 and 90 minutes contains horizontal line segments and no segment with a negative slope.

### QUESTION 2

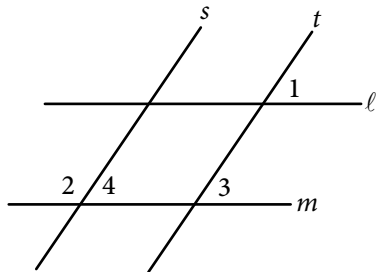
**Choice C is correct.** Substituting 6 for  $x$  and 24 for  $y$  in  $y = kx$  gives  $24 = (k)(6)$ , which gives  $k = 4$ . Hence,  $y = 4x$ . Therefore, when  $x = 5$ , the value of  $y$  is  $(4)(5) = 20$ . None of the other choices for  $y$  is correct because  $y$  is a function of  $x$ , and so there is only one  $y$ -value for a given  $x$ -value.

Choices A, B, and D are incorrect. Choice A is the result of substituting 6 for  $y$  and substituting 5 for  $x$  in the equation  $y = kx$ , when solving for  $k$ . Choice B results from substituting 3 for  $k$  and 5 for  $x$  in the equation  $y = kx$ , when solving for  $y$ . Choice D results from using  $y = k + x$  instead of  $y = kx$ .



### QUESTION 3

**Choice D is correct.** Consider the measures of  $\angle 3$  and  $\angle 4$  in the figure below.



The measure of  $\angle 3$  is equal to the measure of  $\angle 1$  because they are corresponding angles for the parallel lines  $l$  and  $m$  intersected by the transversal line  $t$ . Similarly, the measure of  $\angle 3$  is equal to the measure of  $\angle 4$  because they are corresponding angles for the parallel lines  $s$  and  $t$  intersected by the transversal line  $m$ . Since the measure of  $\angle 1$  is  $35^\circ$ , the measures of  $\angle 3$  and  $\angle 4$  are also  $35^\circ$ . Since  $\angle 4$  and  $\angle 2$  are supplementary angles, the sum of the measures of these two angles is  $180^\circ$ . Therefore, the measure of  $\angle 2$  is  $180^\circ - 35^\circ = 145^\circ$ .

Choice A is incorrect because  $35^\circ$  is the measure of  $\angle 1$ , and  $\angle 1$  is not congruent to  $\angle 2$ . Choice B is incorrect because it is the measure of the complementary angle of  $\angle 1$ , and  $\angle 1$  and  $\angle 2$  are not complementary angles. Choice C is incorrect because it is double the measure of  $\angle 1$ , which cannot be inferred from the information given.

### QUESTION 4

**Choice C is correct.** The description “ $16 + 4x$  is 10 more than 14” can be written as the equation  $16 + 4x = 10 + 14$ , which is equivalent to  $16 + 4x = 24$ . Subtracting 16 from each side of  $16 + 4x = 24$  gives  $4x = 8$ . Since  $8x$  is 2 times  $4x$ , multiplying both sides of  $4x = 8$  by 2 gives  $8x = 16$ . Therefore, the value of  $8x$  is 16.

Choice A is incorrect because it is the value of  $x$ , not  $8x$ . Choices B and D are incorrect and may be the result of errors made when solving the equation  $16 + 4x = 10 + 14$  for  $x$ . For example, choice D could be the result of subtracting 16 from the left side of the equation and adding 16 to the right side of the equation  $16 + 4x = 10 + 14$ , giving  $4x = 40$  and  $8x = 80$ .

### QUESTION 5

**Choice D is correct.** A graph with a strong negative association between  $d$  and  $t$  would have the points on the graph closely aligned with a line that has a negative slope. The more closely the points on a graph are aligned with a line, the stronger the association between  $d$  and  $t$ , and a negative slope indicates a negative association. Of the four graphs, the points on graph D are most closely aligned with a line with a negative slope. Therefore, the graph in choice D has the strongest negative association between  $d$  and  $t$ .

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Choice A is incorrect because the points are more scattered than the points in choice D, indicating a weaker negative association between  $d$  and  $t$ . Choice B is incorrect because the points are aligned to either a curve or possibly a line with a small positive slope. Choice C is incorrect because the points are aligned to a line with a positive slope, indicating a positive association between  $d$  and  $t$ .

## QUESTION 6

**Choice D is correct.** Since there are 10 grams in 1 decagram, there are  $2 \times 10 = 20$  grams in 2 decagrams. Since there are 1,000 milligrams in 1 gram, there are  $20 \times 1,000 = 20,000$  milligrams in 20 grams. Therefore, 20,000 1-milligram doses of the medicine can be stored in a 2-decagram container.

Choice A is incorrect; 0.002 is the number of grams in 2 milligrams. Choice B is incorrect; it could result from multiplying by 1,000 and dividing by 10 instead of multiplying by both 1,000 and 10 when converting from decagrams to milligrams. Choice C is incorrect; 2,000 is the number of milligrams in 2 grams, not the number of milligrams in 2 decagrams.

## QUESTION 7

**Choice C is correct.** Let  $x$  represent the number of installations that each unit on the  $y$ -axis represents. Then  $9x$ ,  $5x$ ,  $6x$ ,  $4x$ , and  $3.5x$  are the number of rooftops with solar panel installations in cities A, B, C, D, and E, respectively. Since the total number of rooftops is 27,500, it follows that  $9x + 5x + 6x + 4x + 3.5x = 27,500$ , which simplifies to  $27.5x = 27,500$ . Thus,  $x = 1,000$ . Therefore, an appropriate label for the  $y$ -axis is “Number of installations (in thousands).”

Choices A, B, and D are incorrect and may result from errors when setting up and calculating the units for the  $y$ -axis.

## QUESTION 8

**Choice D is correct.** If the value of  $|n - 1| + 1$  is equal to 0, then  $|n - 1| + 1 = 0$ . Subtracting 1 from both sides of this equation gives  $|n - 1| = -1$ . The expression  $|n - 1|$  on the left side of the equation is the absolute value of  $n - 1$ , and the absolute value of a quantity can never be negative. Thus  $|n - 1| = -1$  has no solution. Therefore, there are no values for  $n$  for which the value of  $|n - 1| + 1$  is equal to 0.

Choice A is incorrect because  $|0 - 1| + 1 = 1 + 1 = 2$ , not 0. Choice B is incorrect because  $|1 - 1| + 1 = 0 + 1 = 1$ , not 0. Choice C is incorrect because  $|2 - 1| + 1 = 1 + 1 = 2$ , not 0.

## QUESTION 9

**Choice A is correct.** Subtracting 1,052 from both sides of the equation  $a = 1,052 + 1.08t$  gives  $a - 1,052 = 1.08t$ . Then dividing both sides of  $a - 1,052 = 1.08t$  by 1.08 gives  $t = \frac{a - 1,052}{1.08}$ .

Choices B, C, and D are incorrect and could arise from errors in rewriting  $a = 1,052 + 1.08t$ . For example, choice B could result if 1,052 is added to the left side of  $a = 1,052 + 1.08t$  and subtracted from the right side, and then both sides are divided by 1.08.

## QUESTION 10

**Choice B is correct.** The air temperature at which the speed of a sound wave is closest to 1,000 feet per second can be found by substituting 1,000 for  $a$  and then solving for  $t$  in the given formula. Substituting 1,000 for  $a$  in the equation  $a = 1,052 + 1.08t$  gives  $1,000 = 1,052 + 1.08t$ . Subtracting 1,052 from both sides of the equation  $1,000 = 1,052 + 1.08t$  and then dividing both sides of the equation by 1.08 yields

$$t = \frac{-52}{1.08} \approx -48.15. \text{ Of the choices given, } -48^\circ\text{F is closest to } -48.15^\circ\text{F.}$$

Choices A, C, and D are incorrect and might arise from errors made when substituting 1,000 for  $a$  or solving for  $t$  in the equation  $a = 1,052 + 1.08t$  or in rounding the result to the nearest integer. For example, choice C could be the result of rounding  $-48.15$  to  $-49$  instead of  $-48$ .

## QUESTION 11

**Choice A is correct.** Subtracting  $3x$  and adding 3 to both sides of  $3x - 5 \geq 4x - 3$  gives  $-2 \geq x$ . Therefore,  $x$  is a solution to  $3x - 5 \geq 4x - 3$  if and only if  $x$  is less than or equal to  $-2$  and  $x$  is NOT a solution to  $3x - 5 \geq 4x - 3$  if and only if  $x$  is greater than  $-2$ . Of the choices given, only  $-1$  is greater than  $-2$  and, therefore, cannot be a value of  $x$ .

Choices B, C, and D are incorrect because each is a value of  $x$  that is less than or equal to  $-2$  and, therefore, could be a solution to the inequality.

## QUESTION 12

**Choice C is correct.** The average number of seeds per apple is the total number of seeds in the 12 apples divided by the number of apples, which is 12. On the graph, the horizontal axis is the number of seeds per apple and the height of each bar is the number of apples with the corresponding number of seeds. The first bar on the left indicates that 2 apples have 3 seeds each, the second bar indicates that 4 apples have 5 seeds each, the third bar indicates that 1 apple has 6 seeds, the fourth bar indicates that 2 apples have 7 seeds each, and the fifth bar indicates that 3 apples have 9 seeds each. Thus, the total number of seeds for the 12 apples is  $(2 \times 3) + (4 \times 5) + (1 \times 6) + (2 \times 7) + (3 \times 9) = 73$ , and the average number of seeds per apple is  $\frac{73}{12} = 6.08$ . Of the choices given, 6 is closest to 6.08.

Choice A is incorrect; it is the number of apples represented by the tallest bar but is not the average number of seeds for the 12 apples. Choice B is incorrect; it is the number of seeds per apple corresponding to the tallest bar, but is not the average number of seeds for the 12 apples. Choice D is incorrect; a student might choose this value by correctly calculating the average number of seeds, 6.08, but incorrectly rounding up to 7.

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### QUESTION 13

**Choice C is correct.** From the table, there was a total of 310 survey respondents, and 19% of all survey respondents is equivalent to  $\frac{19}{100} \times 310 = 58.9$  respondents. Of the choices given, 59, the number of males taking Geometry, is closest to 58.9 respondents.

Choices A, B, and D are incorrect because the number of males taking Geometry is closer to 58.9 (which is 19% of 310) than the number of respondents in each of these categories.

### QUESTION 14

**Choice C is correct.** The range of the lengths of the 21 fish represented in the table is  $24 - 8 = 16$  inches, and the range of the remaining 20 lengths after the 24-inch measurement is removed is  $16 - 8 = 8$  inches. Therefore, after the 24-inch measurement is removed, the change in range, 8 inches, is much greater than the change in the mean or median.

Choice A is incorrect. Let  $m$  be the mean of the lengths, in inches, of the 21 fish. Then the sum of the lengths, in inches, of the 21 fish is  $21m$ . After the 24-inch measurement is removed, the sum of the lengths, in inches, of the remaining 20 fish is  $21m - 24$ , and the mean length, in inches, of these 20 fish is  $\frac{21m - 24}{20}$ , which is a change of  $\frac{24 - m}{20}$  inches. Since  $m$  must be between the smallest and largest measurements of the 21 fish, it follows that  $8 < m < 24$ , from which it can be seen that the change in the mean, in inches, is between  $\frac{24 - 24}{20} = 0$  and  $\frac{24 - 8}{20} = \frac{4}{5}$ , and so must be less than the change in the range, 8 inches. Choice B is incorrect because the median length of the 21 fish represented in the table is 12, and after the 24-inch measurement is removed, the median of the remaining 20 lengths is also 12. Therefore, the change in the median (0) is less than the change in the range (8). Choice D is incorrect because the changes in the mean, median, and range of the measurements are different.

### QUESTION 15

**Choice A is correct.** The total cost  $C$  of renting a boat is the sum of the initial cost to rent the boat plus the product of the cost per hour and the number of hours,  $h$ , that the boat is rented. The  $C$ -intercept is the point on the  $C$ -axis where  $h$ , the number of hours the boat is rented, is 0. Therefore, the  $C$ -intercept is the initial cost of renting the boat.

Choice B is incorrect because the graph represents the cost of renting only one boat. Choice C is incorrect because the total number of hours of rental is represented by  $h$ -values, each of which corresponds to the first coordinate of a point on the graph not the  $C$ -intercept of the graph. Choice D is incorrect because the increase in cost for each additional hour is given by the slope of the line, not by the  $C$ -intercept.

**QUESTION 16**

**Choice C is correct.** If  $m$  is the slope and  $b$  is the  $C$ -intercept of the line, the relationship between  $h$  and  $C$  can be represented by  $C = mh + b$ . The  $C$ -intercept of the line is 5. Since the points  $(0, 5)$  and  $(1, 8)$  lie on the line, the slope of the line is  $\frac{8-5}{1-0} = \frac{3}{1} = 3$ . Therefore, the relationship between  $h$  and  $C$  can be represented by  $C = 3h + 5$ , the slope-intercept equation of the line.

Choices A and D are incorrect because each of these equations represents a line that passes through the origin  $(0, 0)$ . However,  $C$  is not equal to zero when  $h = 0$ . Choice B is incorrect and may result from errors made when reading the scale on each axis as related to calculating the slope.

**QUESTION 17**

**Choice B is correct.** The minimum value of the function corresponds to the  $y$ -coordinate of the point on the graph that has the smallest  $y$ -coordinate on the graph. Since the smallest  $y$ -coordinate belongs to the point with coordinates  $(-3, -2)$ , the minimum value of the graph is  $f(-3) = -2$ . Therefore, the minimum value of  $f(x)$  is at  $x = -3$ .

Choice A is incorrect;  $-5$  is the least value for an  $x$ -coordinate, not the  $y$ -coordinate, of a point on the graph of  $y = f(x)$ . Choice C is incorrect; it is the minimum value of  $f$ , not the value of  $x$  that corresponds to the minimum of  $f$ . Choice D is incorrect; it is the value of  $x$  for which the value of  $f(x)$  has its maximum, not minimum.

**QUESTION 18**

**Choice A is correct.** Since  $(0, 0)$  is a solution to the system of inequalities, substituting 0 for  $x$  and 0 for  $y$  in the given system must result in two true inequalities. After this substitution,  $y < -x + a$  becomes  $0 < a$ , and  $y > x + b$  becomes  $0 > b$ . Hence,  $a$  is positive and  $b$  is negative. Therefore,  $a > b$ .

Choice B is incorrect because  $b > a$  cannot be true if  $b$  is negative and  $a$  is positive. Choice C is incorrect because it is possible to find an example where  $(0, 0)$  is a solution to the system, but  $|a| < |b|$ ; for example, if  $a = 6$  and  $b = -7$ . Choice D is incorrect because the equation  $a = -b$  doesn't have to be true; for example,  $(0, 0)$  is a solution to the system of inequalities if  $a = 1$  and  $b = -2$ .

**QUESTION 19**

**Choice B is correct.** To determine the number of salads sold, write and solve a system of two equations. Let  $x$  equal the number of salads sold and let  $y$  equal the number of drinks sold. Since a total of 209 salads and drinks were sold, the equation  $x + y = 209$  must hold. Since salads cost \$6.50 each, drinks cost \$2.00 each, and the total revenue from selling  $x$  salads and  $y$  drinks was \$836.50,

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the equation  $6.50x + 2.00y = 836.50$  must also hold. The equation  $x + y = 209$  is equivalent to  $2x + 2y = 418$ , and subtracting  $(2x + 2y)$  from the left-hand side and subtracting 418 from the right-hand side of  $6.50x + 2.00y = 836.50$  gives  $4.5x = 418.50$ . Therefore, the number of salads sold,  $x$ , was  $x = \frac{418.50}{4.50} = 93$ .

Choices A, C, and D are incorrect and could result from errors in writing the equations and solving the system of equations. For example, choice C could have been obtained by dividing the total revenue, \$836.50, by the total price of a salad and a drink, \$8.50, and then rounding up.

## QUESTION 20

**Choice D is correct.** Let  $x$  be the original price of the computer, in dollars. The discounted price is 20 percent off the original price, so  $x - 0.2x = 0.8x$  is the discounted price, in dollars. The sales tax is 8 percent of the discounted price, so  $0.08(0.8x)$  represents the sales tax Alma paid. The price  $p$ , in dollars, that Alma paid the cashiers is the sum of the discounted price and the tax:  $p = 0.8x + (0.08)(0.8x)$  which can be rewritten as  $p = 1.08(0.8x)$ . Therefore, the original price,  $x$ , of the computer, in dollars, can be written as  $\frac{p}{(0.8)(1.08)}$  in terms of  $p$ .

Choices A, B, and C are incorrect. The expression in choice A represents 88% of the amount Alma paid to the cashier, and can be obtained by subtracting the discount of 20% from the original price and adding the sales tax of 8%. However, this is incorrect because 8% of the tax is over the discounted price, not the original one. The expression in choice B is the result of adding the factors associated with the discount and sales tax, 0.8 and .08, rather than multiplying them. The expression in choice C results from assigning  $p$  to represent the original price of the laptop, rather than to the amount Alma paid to the cashier.

## QUESTION 21

**Choice C is correct.** The probability that a person from Group Y who recalled at least 1 dream was chosen at random from the group of all people who recalled at least 1 dream is equal to the number of people in Group Y who recalled at least 1 dream divided by the total number of people in the two groups who recalled at least 1 dream. The number of people in Group Y who recalled at least 1 dream is the sum of the 11 people in Group Y who recalled 1 to 4 dreams and the 68 people in Group Y who recalled 5 or more dreams:  $11 + 68 = 79$ . The total number of people who recalled at least 1 dream is the sum of the 79 people in Group Y who recalled at least 1 dream, the 28 people in Group X who recalled 1 to 4 dreams, and the 57 people in Group X who recalled 5 or more dreams:  $79 + 28 + 57 = 164$ . Therefore, the probability is  $\frac{79}{164}$ .

Choice A is incorrect; it is the probability of choosing at random a person from Group Y who recalled 5 or more dreams. Choice B is incorrect; it is the probability of choosing at random a person from Group Y who recalled at least 1 dream. Choice D is incorrect; it is

the probability of choosing at random a person from the two groups combined who recalled at least 1 dream.

## QUESTION 22

**Choice B is correct.** The amounts given in the table are in thousands of dollars. Therefore, the amount in the annual budget for agriculture/natural resources is actually \$488,106,000 in 2010 and \$358,708,000 in 2008. Therefore, the change in the budgeted amount is  $\$488,106,000 - \$358,708,000 = \$129,398,000$ . Hence, the average change in the annual budget for agriculture/natural resources from 2008 to 2010 is  $\frac{\$129,398,000}{2} = \$64,699,000$  per year. Of the options given, this average rate of change is closest to \$65,000,000 per year.

Choices A and C are incorrect and may result from errors in setting up or calculating the average rate of change. Choice D is incorrect; \$130,000,000 is the approximate total change in the annual budget for agriculture/natural resources from 2008 to 2010, not the average rate of change from 2008 to 2010.

## QUESTION 23

**Choice B is correct.** The human resources budget in 2007 was 4,051,050 thousand dollars, and the human resources budget in 2010 was 5,921,379 thousand dollars. Therefore, the ratio of the 2007 budget to the 2010 budget is slightly greater than  $\frac{4}{6} = \frac{2}{3}$ . Similar estimates for agriculture/natural resources give a ratio of the 2007 budget to the 2010 budget of slightly greater than  $\frac{3}{4}$ ; for education, a ratio of slightly greater than  $\frac{2}{3}$ ; for highways and transportation, a ratio of slightly less than  $\frac{5}{6}$ ; and for public safety, a ratio of slightly greater than  $\frac{5}{9}$ .

Therefore, of the given choices, education's ratio of the 2007 budget to the 2010 budget is closest to that of human resources.

Choices A, C, and D are incorrect because the ratio of the 2007 budget to 2010 budget for each of the programs given in these choices is further from the corresponding ratio for human resources than the corresponding ratio for education.

## QUESTION 24

**Choice A is correct.** The equation of a circle can be written as  $(x - h)^2 + (y - k)^2 = r^2$  where  $(h, k)$  are the coordinates of the center of the circle and  $r$  is the radius of the circle. Since the coordinates of the center of the circle are  $(0, 4)$ , the equation of the circle is  $x^2 + (y - 4)^2 = r^2$ . The radius of the circle is the distance from the center,  $(0, 4)$ , to the given endpoint of a radius,  $(\frac{4}{3}, 5)$ . By the distance formula,  $r^2 = (\frac{4}{3} - 0)^2 + (5 - 4)^2 = \frac{25}{9}$ . Therefore, an equation of the given circle is  $x^2 + (y - 4)^2 = \frac{25}{9}$ .

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Choices B and D are incorrect. The equations given in these choices represent a circle with center  $(0, -4)$ , not  $(0, 4)$ . Choice C is incorrect; it results from using  $r$  instead of  $r^2$  in the equation for the circle.

### QUESTION 25

**Choice D is correct.** When the ball hits the ground, its height is 0 meters. Substituting 0 for  $h$  in  $h = -4.9t^2 + 25t$  gives  $0 = -4.9t^2 + 25t$ , which can be rewritten as  $0 = t(-4.9t + 25)$ . Thus, the possible values of  $t$  are  $t = 0$  and  $t = \frac{25}{4.9} \approx 5.1$ . The time  $t = 0$  seconds corresponds to the time the ball is launched from the ground, and the time  $t \approx 5.1$  seconds corresponds to the time after launch that the ball hits the ground. Of the given choices, 5.0 seconds is closest to 5.1 seconds, so the ball returns to the ground approximately 5.0 seconds after it is launched.

Choice A, B, and C are incorrect and could arise from conceptual or computation errors while solving  $0 = -4.9t^2 + 25t$  for  $t$ .

### QUESTION 26

**Choice B is correct.** Let  $x$  represent the number of pears produced by the Type B trees. Type A trees produce 20 percent more pears than Type B trees, or  $x$ , which can be represented as  $x + 0.20x = 1.20x$  pears. Since Type A trees produce 144 pears, it follows that  $1.20x = 144$ . Thus  $x = \frac{144}{1.20} = 120$ . Therefore, the Type B trees produced 120 pears.

Choice A is incorrect because while 144 is reduced by approximately 20 percent, increasing 115 by 20 percent gives 138, not 144. Choice C is incorrect; it results from subtracting 20 from the number of pears produced by the Type A trees. Choice D is incorrect; it results from adding 20 percent of the number of pears produced by Type A trees to the number of pears produced by Type A trees.

### QUESTION 27

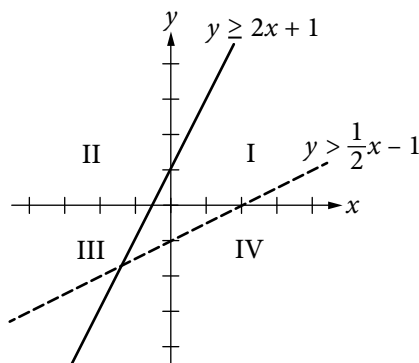
**Choice C is correct.** The area of the field is 100 square meters. Each 1-meter-by-1-meter square has an area of 1 square meter. Thus, on average, the earthworm counts to a depth of 5 centimeters for each of the regions investigated by the students should be about  $\frac{1}{100}$  of the total number of earthworms to a depth of 5 centimeters in the entire field. Since the counts for the smaller regions are from 107 to 176, the estimate for the entire field should be between 10,700 and 17,600. Therefore, of the given choices, 15,000 is a reasonable estimate for the number of earthworms to a depth of 5 centimeters in the entire field.

Choice A is incorrect; 150 is the approximate number of earthworms in 1 square meter. Choice B is incorrect; it results from using 10 square meters as the area of the field. Choice D is incorrect; it results from using 1,000 square meters as the area of the field.



## QUESTION 28

**Choice C is correct.** To determine which quadrant does not contain any solutions to the system of inequalities, graph the inequalities. Graph the inequality  $y \geq 2x + 1$  by drawing a line through the  $y$ -intercept  $(0, 1)$  and the point  $(1, 3)$ , as shown. The solutions to this inequality are all points contained on and above this line. Graph the inequality  $y > \frac{1}{2}x - 1$  by drawing a dashed line through the  $y$ -intercept  $(0, -1)$  and the point  $(2, 0)$ , as shown. The solutions to this inequality are all points above this dashed line.



The solution to the system of inequalities is the intersection of the regions above the graphs of both lines. It can be seen that the solutions only include points in quadrants I, II, and III and do not include any points in quadrant IV.

Choices A and B are incorrect because quadrants II and III contain solutions to the system of inequalities, as shown in the figure above. Choice D is incorrect because there are no solutions in quadrant IV.

## QUESTION 29

**Choice D is correct.** If the polynomial  $p(x)$  is divided by  $x - 3$ , the result can be written as  $\frac{p(x)}{x-3} = q(x) + \frac{r}{x-3}$ , where  $q(x)$  is a polynomial and  $r$  is the remainder. Since  $x - 3$  is a degree 1 polynomial, the remainder is a real number. Hence,  $p(x)$  can be written as  $p(x) = (x - 3)q(x) + r$ , where  $r$  is a real number. It is given that  $p(3) = -2$  so it must be true that  $-2 = p(3) = (3 - 3)q(3) + r = (0)q(3) + r = r$ . Therefore, the remainder when  $p(x)$  is divided by  $x - 3$  is  $-2$ .

Choice A is incorrect because  $p(3) = -2$  does not imply that  $p(5) = 0$ . Choices B and C are incorrect because the remainder  $-2$  or its opposite,  $2$ , need not be a root of  $p(x)$ .

## QUESTION 30

**Choice D is correct.** Any quadratic function  $q$  can be written in the form  $q(x) = a(x - h)^2 + k$ , where  $a$ ,  $h$ , and  $k$  are constants and  $(h, k)$  is the vertex of the parabola when  $q$  is graphed in the coordinate plane. This form can be reached by completing the square in the expression that defines  $q$ . The equation of the graph is  $y = x^2 - 2x - 15$ .

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Since the coefficient of  $x$  is  $-2$ , this equation can be written in terms of  $(x - 1)^2 = x^2 - 2x + 1$  as follows:  $y = x^2 - 2x - 15 = (x^2 - 2x + 1) - 16 = (x - 1)^2 - 16$ . From this form of the equation, the coefficients of the vertex can be read as  $(1, -16)$ .

Choices A and C are incorrect because the coordinates of the vertex A do not appear as constants in these equations. Choice B is incorrect because it is not equivalent to the given equation.

### QUESTION 31

**The correct answer is any number between 4 and 6, inclusive.** Since Wyatt can husk at least 12 dozen ears of corn per hour, it will take him no more than  $\frac{72}{12} = 6$  hours to husk 72 dozen ears of corn. On the other hand, since Wyatt can husk at most 18 dozen ears of corn per hour, it will take him at least  $\frac{72}{18} = 4$  hours to husk 72 dozen ears of corn.

Therefore, the possible times it could take Wyatt to husk 72 dozen ears of corn are 4 hours to 6 hours, inclusive. Any number between 4 and 6, inclusive, can be gridded as the correct answer.

### QUESTION 32

**The correct answer is 107.** Since the weight of the empty truck and its driver is 4500 pounds and each box weighs 14 pounds, the weight, in pounds, of the delivery truck, its driver, and  $x$  boxes is  $4500 + 14x$ . This weight is below the bridge's posted weight limit of 6000 pounds if  $4500 + 14x < 6000$ . Subtracting 4500 from both sides of this inequality and then dividing both sides by 14 yields  $x < \frac{1500}{14}$  or  $x < 107\frac{1}{7}$ . Since the number of packages must be an integer, the maximum possible value for  $x$  that will keep the combined weight of the truck, its driver, and the  $x$  identical boxes below the bridge's posted weight limit is 107.

### QUESTION 33

**The correct answer is  $\frac{5}{8}$  or .625.** Based on the line graph, the number of portable media players sold in 2008 was 100 million, and the number of portable media players sold in 2011 was 160 million. Therefore, the number of portable media players sold in 2008 is  $\frac{100 \text{ million}}{160 \text{ million}}$  of the portable media players sold in 2011. This fraction reduces to  $\frac{5}{8}$ . Either  $\frac{5}{8}$  or its decimal equivalent, .625, may be gridded as the correct answer.

**QUESTION 34**

**The correct answer is 96.** Since each day has a total of 24 hours of time slots available for the station to sell, there is a total of 48 hours of time slots available to sell on Tuesday and Wednesday. Each time slot is a 30-minute interval, which is equal to a  $\frac{1}{2}$ -hour interval. Therefore,

there are  $\frac{48 \text{ hours}}{\frac{1}{2} \text{ hours/time slot}} = 96$  time slots of 30 minutes for the station

to sell on Tuesday and Wednesday.

**QUESTION 35**

**The correct answer is 6.** The volume of a cylinder is  $\pi r^2 h$ , where  $r$  is the radius of the base of the cylinder and  $h$  is the height of the cylinder. Since the storage silo is a cylinder with volume  $72\pi$  cubic yards and height 8 yards, it follows that  $72\pi = \pi r^2(8)$ , where  $r$  is the radius of the base of the cylinder, in yards. Dividing both sides of the equation  $72\pi = \pi r^2(8)$  by  $8\pi$  gives  $r^2 = 9$ , and so the radius of the base of the cylinder is 3 yards. Therefore, the diameter of the base of the cylinder is 6 yards.

**QUESTION 36**

**The correct answer is 3.** The function  $h(x)$  is undefined when the denominator of  $\frac{1}{(x-5)^2 + 4(x-5) + 4}$  is equal to zero. The expression  $(x-5)^2 + 4(x-5) + 4$  is a perfect square:  $(x-5)^2 + 4(x-5) + 4 = ((x-5) + 2)^2$ , which can be rewritten as  $(x-3)^2$ . The expression  $(x-3)^2$  is equal to zero if and only if  $x = 3$ . Therefore, the value of  $x$  for which  $h(x)$  is undefined is 3.

**QUESTION 37**

**The correct answer is 1.02.** The initial deposit earns 2 percent interest compounded annually. Thus at the end of 1 year, the new value of the account is the initial deposit of \$100 plus 2 percent of the initial deposit:  $\$100 + \frac{2}{100}(\$100) = \$100(1.02)$ . Since the interest is compounded annually, the value at the end of each succeeding year is the sum of the previous year's value plus 2 percent of the previous year's value. This is again equivalent to multiplying the previous year's value by 1.02. Thus, after 2 years, the value will be  $\$100(1.02)(1.02) = \$100(1.02)^2$ ; after 3 years, the value will be  $\$100(1.02)^3$ ; and after  $t$  years, the value will be  $\$100(1.02)^t$ . Therefore, in the formula for the value for Jessica's account after  $t$  years,  $\$100(x)^t$ , the value of  $x$  must be 1.02.

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## QUESTION 38

**The correct answer is 6.11.** Jessica made an initial deposit of \$100 into her account. The interest on her account is 2 percent compounded annually, so after 10 years, the value of her initial deposit has been multiplied 10 times by the factor  $1 + 0.02 = 1.02$ . Hence, after 10 years, Jessica's deposit is worth  $\$100(1.02)^{10} = \$121.899$  to the nearest tenth of a cent. Tyshaun made an initial deposit of \$100 into his account. The interest on his account is 2.5 percent compounded annually, so after 10 years, the value of his initial deposit has been multiplied 10 times by the factor  $1 + 0.025 = 1.025$ . Hence, after 10 years, Tyshaun's deposit is worth  $\$100(1.025)^{10} = \$128.008$  to the nearest tenth of a cent. Hence, Jessica's initial deposit earned \$21.899 and Tyshaun's initial deposit earned \$28.008. Therefore, to the nearest cent, Tyshaun's initial deposit earned \$6.11 more than Jessica's initial deposit.